

A Study on Multi-Objective Emergency Transportation Problem Using Neutrosophic Fuzzy Set

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In this paper, the several Multi-Objective Transportation Problem (MOTP) techniques are applied to solve real life problems. The objective of this application is to select the best transportation path with minimum time and cost as well as maximum man power and fund to the landslide affected area peoples. MOTP methodology has treated as a large number of successful applications in a variety of fields, like industrial location, investments, manpower planning, tourism, and so on. The victory of this technique is primarily due to its mathematical properties and its particular friendliness.

1. Introduction

Transportation Problems (TP) was analysed and introduced by Hitchcock (1941). These transportation problems are associated with single objective. But mostly in real-life situations, transportation problem usually involves multiple, conflicting, and imprecise parameters. For this type of problem there exists a technique, Multi-Objective Transportation Problem (MOTP). It is more difficult to solve because of the conflict and imprecise nature. To overcome this difficulty, Fuzzy Set Theory (FST) was developed by Zadeh (1965).

2. Multi-Objective Transportation Problem under Neutrosophic Environment

Defining the problem in the form of Neutrosophic fuzzy set as

$$D_N = \left(\bigcap_{i=1}^m O_i \right) \left(\bigcap_{j=1}^n C_j \right) (x, M_D(x), F_D(x), T_D(x))$$

Where $O_i \rightarrow$ neutrosophic objectives;

$C_i \rightarrow$ neutrosophic constrains;

$M_D \rightarrow$ truth membership grade ;

$F_D \rightarrow$ indeterminacy membership grade;

$T_D \rightarrow$ falsity membership grade.

$$M_D(x) = \max \left\{ \begin{matrix} M_{o1}(x), M_{o2}(x), \dots, M_{om}(x); \\ M_{c1}(x), M_{c2}(x), \dots, M_{cn}(x) \end{matrix} \right\} \forall x \in X$$

$$F_D(x) = \max \left\{ \begin{matrix} F_{o1}(x), F_{o2}(x), \dots, F_{om}(x); \\ F_{c1}(x), F_{c2}(x), \dots, F_{cn}(x) \end{matrix} \right\} \forall x \in X$$

$$T_D(x) = \min \left\{ \begin{matrix} T_{o1}(x), T_{o2}(x), \dots, T_{om}(x); \\ T_{c1}(x), T_{c2}(x), \dots, T_{cn}(x) \end{matrix} \right\} \forall x \in X$$

For formulating the membership values, need to find an upper (U_K) and lower (L_K) bounds for each objective function and is defined as follows

$$U_K = \max\{H_K(x)\}_{K=1}^K \text{ and}$$

$$L_K = \min\{H_K(x)\}_{K=1}^K$$

Then, with the help of bounded values, the membership values are determined as follows

$$M_K(Z_K(x)) = \begin{cases} 1 & Z_K(x) \leq L_K^M \\ 1 - \frac{Z_K(x) - L_K^M}{U_K^M - L_K^M} & L_K^M \leq Z_K(x) \leq U_K^M \\ 0 & Z_K(x) \geq U_K^M \end{cases}$$

$$F_K(Z_K(x)) = \begin{cases} 1 & Z_K(x) \leq L_K^F \\ 1 - \frac{Z_K(x) - L_K^F}{U_K^F - L_K^F} & L_K^F \leq Z_K(x) \leq U_K^F \\ 0 & Z_K(x) \geq U_K^F \end{cases}$$

$$T_K(Z_K(x)) = \begin{cases} 1 & Z_K(x) \geq L_K^T \\ 1 - \frac{L_K^T - Z_K(x)}{U_K^T - L_K^T} & L_K^T \leq Z_K(x) \leq U_K^T \\ 0 & Z_K(x) \leq U_K^T \end{cases}$$

3. EXAMPLE PROBLEM:

After a landslide, the community welfare team has shipped their units of

- i) Man power
- ii) Fund for food and water items
- iii) Health supplies like medicine and sanitation etc.,

From their welfare centres S1, S2, S3 to most affected landslide areas D1, D2, D3, D4 respectively with the following characteristics; the transportation cost, time, and loss of deterioration are considered as Neutrosophic penalties.

Supplies: 7,18,16

Demand: 10, 2, 13,15

Penalties:

Category 1:

$$C_1 = \begin{bmatrix} (0.5,0.4,0.6) & (0.4,0.4,0.5) & (0.5,0.3,0.7) & (0.5,0.5,0.4) \\ (0.5,0.3,0.6) & (0.3,0.1,0.2) & (0.6,0.7,0.3) & (0.5,0.4,0.6) \\ (0.6,0.5,0.3) & (0.6,0.7,0.4) & (0.4,0.4,0.5) & (0.6,0.4,0.3) \end{bmatrix}$$

Category 2:

$$C_2 = \begin{bmatrix} (0.4,0.4,0.5) & (0.4,0.3,0.7) & (0.5,0.6,0.3) & (0.6,0.5,0.2) \\ (0.4,0.3,0.6) & (0.6,0.5,0.7) & (0.5,0.2,0.6) & (0.6,0.4,0.3) \\ (0.6,0.5,0.2) & (0.7,0.6,0.4) & (0.3,0.7,0.3) & (0.5,0.3,0.7) \end{bmatrix}$$

Objective function for the above problem is as follows

$$\text{Max}M_1(U(u)) = 0.5u_{11} + 0.4u_{12} + 0.5u_{13} + 0.5u_{14} + 0.5u_{21} + 0.3u_{22} + 0.6u_{23} \\ + 0.5u_{24} + 0.6u_{31} + 0.6u_{32} + 0.4u_{33} + 0.6u_{34}$$

$$\text{Max}M_2(V(v)) = 0.4v_{11} + 0.4v_{12} + 0.5v_{13} + 0.6v_{14} + 0.4v_{21} + 0.6v_{22} + 0.5v_{23} + 0.6v_{24} \\ + 0.6v_{31} + 0.7v_{32} + 0.3v_{33} + 0.5v_{34}$$

$$\text{Max}F_1(U(u)) = 0.4u_{11} + 0.4u_{12} + 0.3u_{13} + 0.5u_{14} + 0.3u_{21} + 0.1u_{22} + 0.7u_{23} + 0.4u_{24} \\ + 0.5u_{31} + 0.7u_{32} + 0.4u_{33} + 0.4u_{34}$$

$$\text{Max}F_2(V(v)) = 0.4v_{11} + 0.3v_{12} + 0.6v_{13} + 0.5v_{14} + 0.3v_{21} + 0.5v_{22} + 0.2v_{23} + 0.4v_{24} \\ + 0.5v_{31} + 0.6v_{32} + 0.7v_{33} + 0.3v_{34}$$

$$\text{Min}T_1(U(u)) = 0.6u_{11} + 0.5u_{12} + 0.7u_{13} + 0.4u_{14} + 0.6u_{21} + 0.2u_{22} + 0.3u_{23} + 0.6u_{24} \\ + 0.3u_{31} + 0.4u_{32} + 0.5u_{33} + 0.3u_{34}$$

$$\text{Min}T_2(V(v)) = 0.5v_{11} + 0.7v_{12} + 0.3v_{13} + 0.2v_{14} + 0.6v_{21} + 0.7v_{22} + 0.6v_{23} + 0.3v_{24} \\ + 0.2v_{31} + 0.4v_{32} + 0.3v_{33} + 0.7v_{34}$$

Then, separating the membership function in matrix format as shown below

$$M_1 = \begin{bmatrix} 0.5 & 0.4 & 0.5 & 0.5 \\ 0.5 & 0.3 & 0.6 & 0.5 \\ 0.6 & 0.6 & 0.4 & 0.6 \end{bmatrix} \& M_2 = \begin{bmatrix} 0.4 & 0.4 & 0.5 & 0.6 \\ 0.4 & 0.6 & 0.5 & 0.6 \\ 0.6 & 0.7 & 0.3 & 0.5 \end{bmatrix}$$

$$F_1 = \begin{bmatrix} 0.4 & 0.4 & 0.3 & 0.5 \\ 0.3 & 0.1 & 0.7 & 0.4 \\ 0.5 & 0.7 & 0.4 & 0.4 \end{bmatrix} \& F_2 = \begin{bmatrix} 0.4 & 0.3 & 0.6 & 0.5 \\ 0.3 & 0.5 & 0.2 & 0.4 \\ 0.5 & 0.6 & 0.7 & 0.3 \end{bmatrix}$$
$$T_1 = \begin{bmatrix} 0.6 & 0.5 & 0.7 & 0.4 \\ 0.6 & 0.2 & 0.3 & 0.6 \\ 0.3 & 0.4 & 0.5 & 0.3 \end{bmatrix} \& T_2 = \begin{bmatrix} 0.5 & 0.7 & 0.3 & 0.2 \\ 0.6 & 0.7 & 0.6 & 0.3 \\ 0.2 & 0.4 & 0.3 & 0.7 \end{bmatrix}$$

Now, evaluating the membership values and we get

$$M_1 = \begin{bmatrix} 0.5 & 0.4 & 0.5 & 0.5 \\ 0.5 & 0.3 & 0.6 & 0.5 \\ 0.6 & 0.6 & 0.4 & 0.6 \end{bmatrix}; U_1^M = 0.6 \& L_1^M = 0.3$$
$$M_2 = \begin{bmatrix} 0.4 & 0.4 & 0.5 & 0.6 \\ 0.4 & 0.6 & 0.5 & 0.6 \\ 0.6 & 0.7 & 0.3 & 0.5 \end{bmatrix}; U_2^M = 0.7 \& L_2^M = 0.3$$

We get the truth membership values as given below

$$M_1(U(u)) = \begin{bmatrix} 0.33 & 0.67 & 0.33 & 0.33 \\ 0.33 & 1 & 0 & 0.33 \\ 0 & 0 & 0.67 & 0 \end{bmatrix} \&$$
$$M_2(V(v)) = \begin{bmatrix} 0.75 & 0.75 & 0.50 & 0.25 \\ 0.75 & 0.25 & 0.50 & 0.25 \\ 0.25 & 0 & 1 & 0.50 \end{bmatrix}$$

From above two matrices, we get a truth membership matrix as

	D1	D2	D3	D4	Supply
S1	0.75	0.67	0.50	0.33	7
S2	0.75	1	0.50	0.33	18
S3	0.25	0	1	0.50	16
Demand	10	2	13	15	

Table 2.1: Truth Membership Matrix

Now taking the indeterminacy values

$$F_1 = \begin{bmatrix} 0.4 & 0.4 & 0.3 & 0.5 \\ 0.3 & 0.1 & 0.7 & 0.4 \\ 0.5 & 0.7 & 0.4 & 0.4 \end{bmatrix}; U_1^F = 0.7 \& L_1^F = 0.1$$
$$F_2 = \begin{bmatrix} 0.4 & 0.3 & 0.6 & 0.5 \\ 0.3 & 0.5 & 0.2 & 0.4 \\ 0.5 & 0.6 & 0.7 & 0.3 \end{bmatrix}; U_1^F = 0.7 \& L_1^F = 0.2$$

We get the indeterminacy membership values as given below

$$F_1(U(u)) = \begin{bmatrix} 0.5 & 0.5 & 0.67 & 0.3 \\ 0.67 & 1 & 0 & 0.5 \\ 0.3 & 0 & 0.5 & 0.5 \end{bmatrix} \&$$

$$F_2(V(v)) = \begin{bmatrix} 0.6 & 0.8 & 0.2 & 0.4 \\ 0.8 & 0.4 & 1 & 0.6 \\ 0.4 & 0.2 & 0 & 0.8 \end{bmatrix}$$

From above two matrices, we get a indeterminacy membership matrix as

	D1	D2	D3	D4	Supply
S1	0.6	0.8	0.67	0.4	7
S2	0.8	1	1	0.6	18
S3	0.4	0.2	0.5	0.8	16
Demand	10	2	13	15	

Table 2.2: indeterminacy membership matrix

Now taking the falsity values

$$T_1 = \begin{bmatrix} 0.6 & 0.5 & 0.7 & 0.4 \\ 0.6 & 0.2 & 0.3 & 0.6 \\ 0.3 & 0.4 & 0.5 & 0.3 \end{bmatrix}; U_1^T = 0.7 \& L_1^T = 0.2$$

$$T_2 = \begin{bmatrix} 0.5 & 0.7 & 0.3 & 0.2 \\ 0.6 & 0.7 & 0.6 & 0.3 \\ 0.2 & 0.4 & 0.3 & 0.7 \end{bmatrix}; U_1^T = 0.7 \& L_1^T = 0.2$$

We get the falsity membership values as given below

$$T_1(U(u)) = \begin{bmatrix} 0.8 & 0.6 & 1 & 0.4 \\ 0.8 & 0 & 0.20 & 0.8 \\ 0.2 & 0.4 & 0.6 & 0.2 \end{bmatrix} \&$$

$$T_2(V(v)) = \begin{bmatrix} 0.6 & 1 & 0.2 & 0 \\ 0.8 & 1 & 0.8 & 0.2 \\ 0 & 0.4 & 0.2 & 1 \end{bmatrix}$$

From above two matrices, we get a falsity membership matrix as

	D1	D2	D3	D4	Supply
S1	0.6	0.6	0.2	0	7
S2	0.8	0	0.20	0.2	18
S3	0	0.4	0.2	0.2	16
Demand	10	2	13	15	

Table 2.3: Falsity Membership Matrix

Solving the tables 2.1,2.2,2.3 separately by VAM method, we get the values,

	VAM
M	27.96
F	33.6
T	4.2

4. CONCLUSION:

The above results show that the maximum man power and fund (M and F) for transportation to supply food, water and health supplies like medicine and so on. And minimize the travelling time (T) to help the landslide affected area peoples in correct time. A natural disaster is an unexpected occurrence of events that harm society. Some of them are earthquake, tsunami, landslide, flood, volcanic eruption, cyclone, and so on. the main motive is to provide an optimal solution for a transportation problem with multiple objective functions in any emergency situation.

References

1. Snekaa B, Porchelvi RS. Application of fuzzy soft set theory and Hungarian method for assigning player’s position. *Malaya Journal of Matematik*. 2020 Oct 1;8(04):1661-4.

2. Hepzibah RI, Emimal S. On Solving Neutrosophic Unconstrained Optimization Problems by Steepest Descent Method and Fletcher Reeves Method. *International Journal of Fuzzy Mathematical Archive*. 2021;19(2):111-22.

3. Veeramani C, Edalatpanah SA, Sharanya S. Solving the multi objective fractional transportation problem through the neutrosophic goal programming approach. *Discrete dynamics in nature and society*. 2021 Aug 30;2021:1-7.

4. Singh A, Arora R, Arora S. Bilevel transportation problem in neutrosophic environment. *Computational and Applied Mathematics*. 2022 Feb;41:1-25. Joshi VD, Singh J, Saini R, Nisar KS. Solving multi-objective linear fractional transportation problem under neutrosophic environment. *Journal of Interdisciplinary Mathematics*. 2022 Jan 2; 25(1):123-36.

5. Giri BK, Roy SK. Neutrosophic multi-objective green four-dimensional fixed-charge transportation problem. *International Journal of Machine Learning and Cybernetics*. 2022 Oct;13(10):3089-112. Mardanya D, Roy SK. New approach to solve fuzzy multi-objective multi-item solid transportation problem. *RAIRO-Operations Research*. 2023 Jan 1;57(1):99-120

6. V. , Maheswari U. , K. G. [2024]. A New Approach to Solve Transportation Problems Under Neutrosophic Environment. *Journal of International Journal of Neutrosophic Science*. 23(4): 224- 237

7. Gupta G, Shivani, Rani D. Neutrosophic goal programming approach for multi-objective fixed-charge transportation problem with neutrosophic parameters. *OPSEARCH*. 2024 Feb 20:1-27.